

# Lifetime Model for Solder Layers

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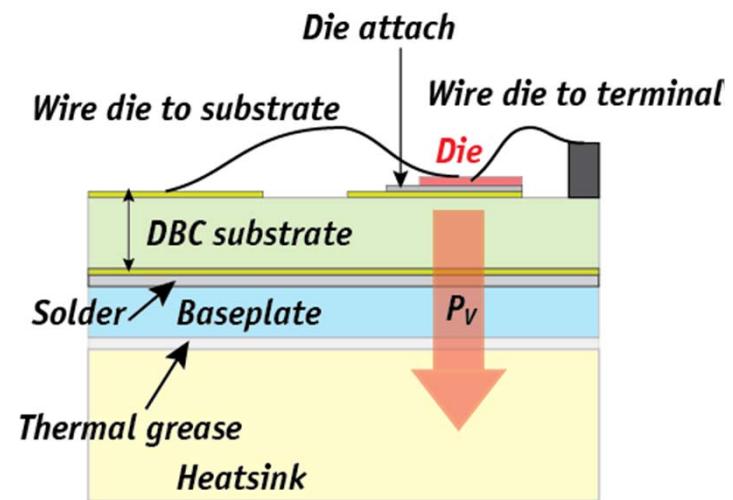
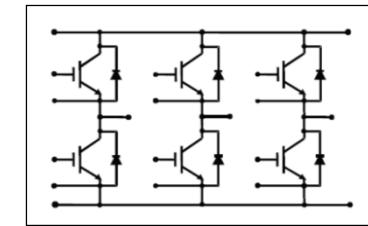


# Overview

- Reliability of Power Modules
- Failure Mechanism of Power Modules
  - *Power Cycling (PC) tests, Temperature Cycling (TC) tests*
- Analytical vs. Physical Lifetime Modeling
- Physical lifetime model based on Clech's algorithm for Solder Interconnections
- Solder Interconnection Failure
  - *Solder equations (elastic, plastic and creep deformation)*
  - *Energy-based modeling*
- Lifetime Estimation based on PC tests

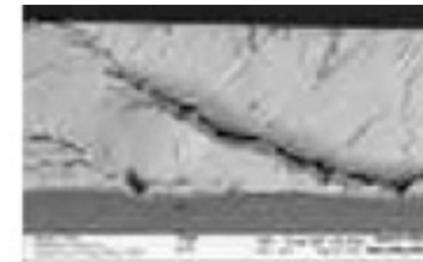
# Reliability of Power Modules

- Power Module: layers with typically different thermal constants have great influence on heating and cooling rate of module
- Thermo-mechanical Stress: temperature gradients and *CTE* (Coefficient of Thermal Expansion) difference between layers
- Mission Profile
- Lifetime Modeling

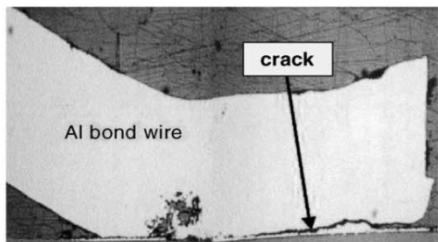


# Failure of Power Modules

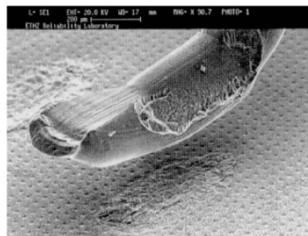
- Bond wire fatigue (lift off, heel cracking)
- Aluminium reconstruction
- Brittle cracking, fatigue crack propagation
- Corrosion of interconnections
- Solder fatigue
- Burnout failures



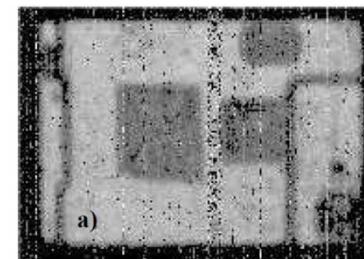
Ref [D. C. Katsis, "Thermal Characterization of Die-Attach Degradation in the Power MOSFET"]



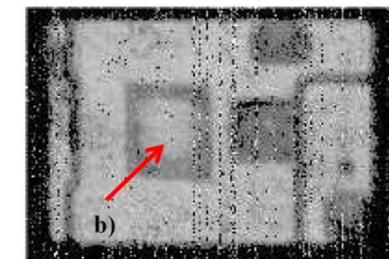
Ref [Lefranc, G., et al. (2003) "Aluminium bond-wire properties after 1 billion cycles"]



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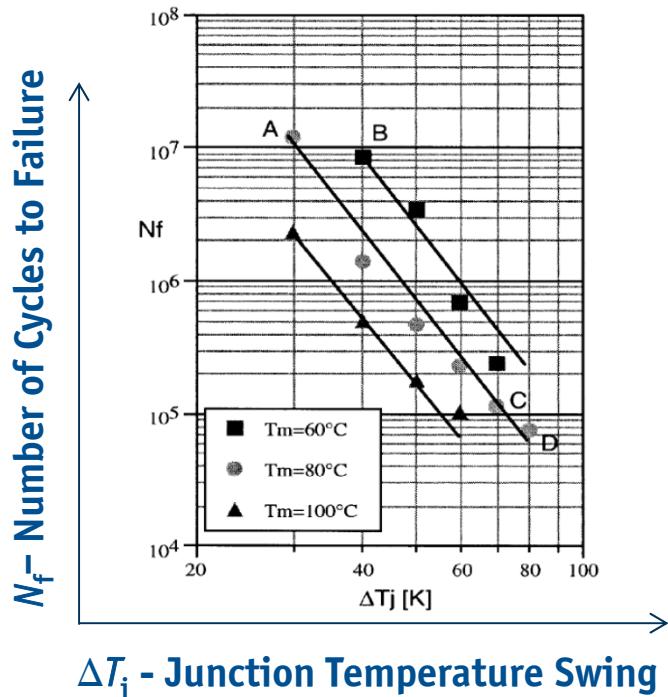


Ref [U. Scheuermann, R. Schmidt (EPE 2011), "Impact of Solder Fatigue on Module Lifetime in Power Cycling Tests"]



## Lifetime Modeling – Analytical Models

### ■ Basic $N_f$ Model: Coffin-Manson

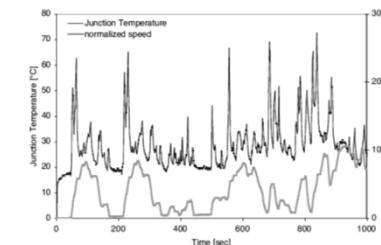


$$N_f = a \cdot (\Delta T_{\text{cyc}})^{-n}$$

$$N_f = a \cdot (\Delta T_{\text{cyc}})^{-n} \exp\left(\frac{E_A}{k_B T_{\text{jm}}}\right)$$

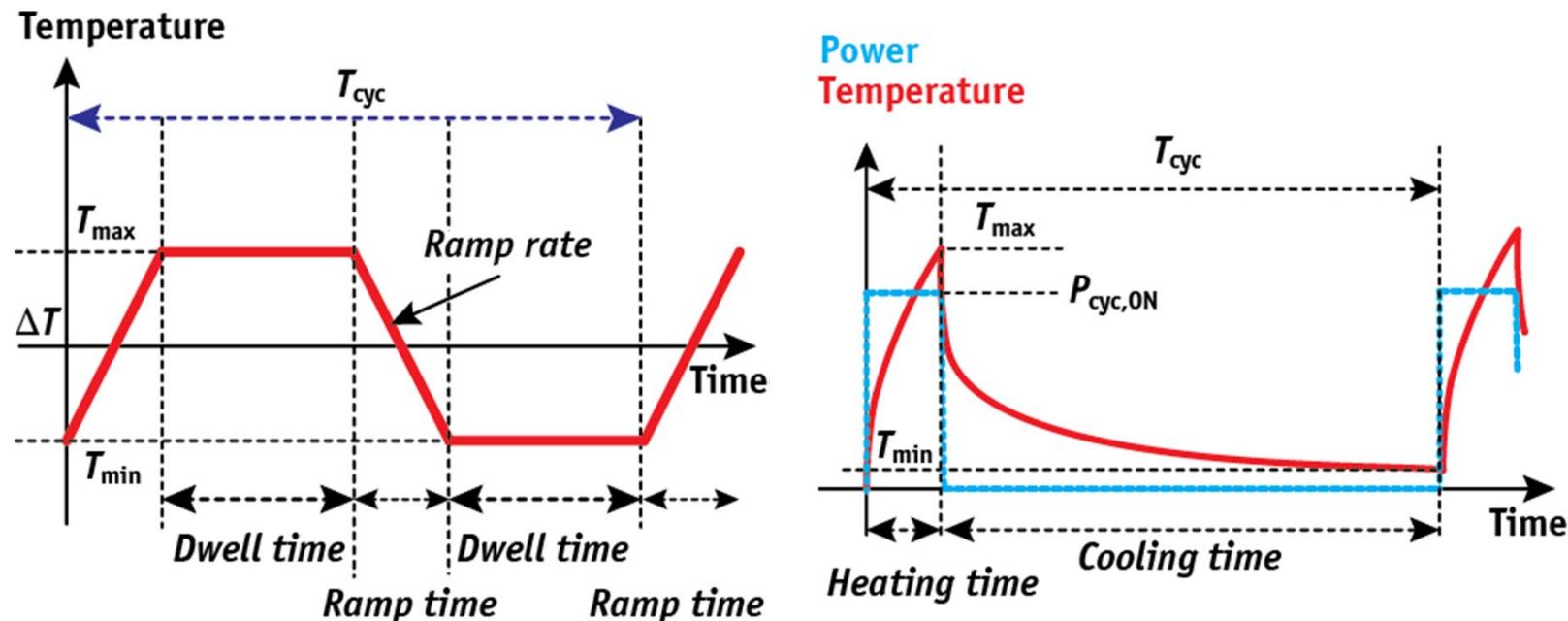
**Rain Flow Algorithm**  
(counting  $\Delta T_{\text{cyc}}$  in mission profile)  
+ Miner's rule

$$\frac{1}{MTTF} = \sum \frac{n_i}{N_{fi}}$$



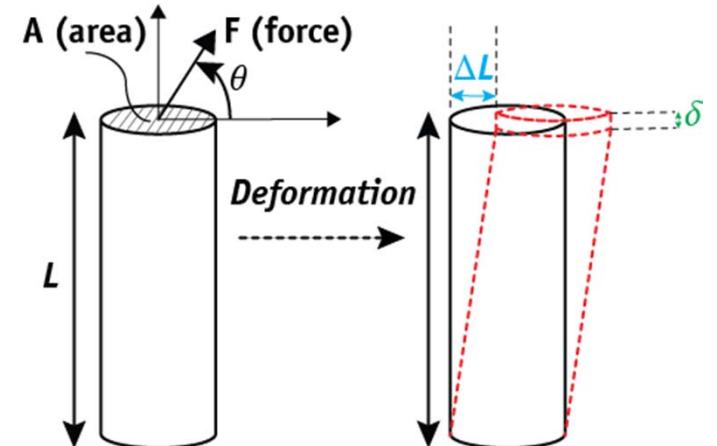
# Accelerated Power Cycling Tests

## ■ Accelerated Power Cycling Tests



## Lifetime Modeling – Physical Models

- Failure and deformation mechanism have to be known in advance
  - \* Bond Wire Lift-off : Crack Propagation
  - \* Solder Failure: Stress-/Strain-/Damage /Energy-based model
- Thermo-mechanical behaviour: stress ( $\tau, \sigma$ ) and strain ( $\gamma, \epsilon$ )



$$\text{Normal Stress } \sigma = F \sin \theta / A$$

$$\text{Normal Strain } \epsilon = \delta / L$$

$$\text{Shear Stress } \tau = F \cos \theta / A$$

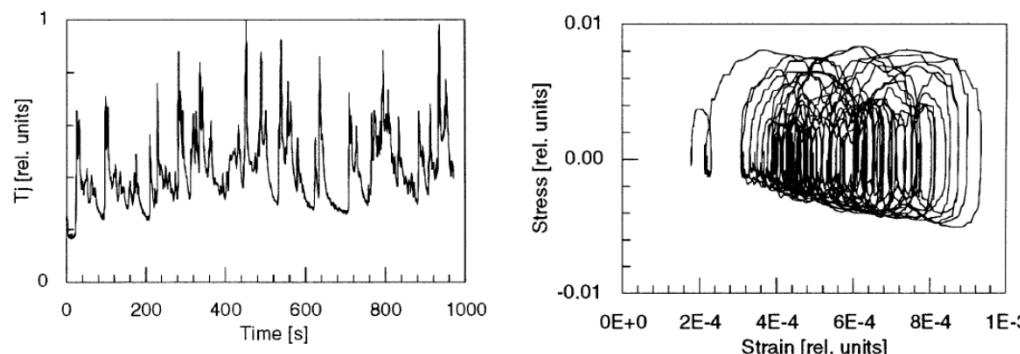
$$\text{Shear Strain } \gamma = \Delta L / L$$

## Physical Lifetime Modeling

$$N_f = f(\Delta\gamma), f(\Delta\tau), f(\Delta D), f(\Delta W)$$

$$\frac{da}{dN} = K_1 (\Delta W)^{K_2}$$
$$N_f = \frac{1}{2} \left[ \frac{\Delta\gamma}{2\epsilon'_f} \right]^{1/c}$$
$$\Delta W \cdot (N_f)^m = K$$

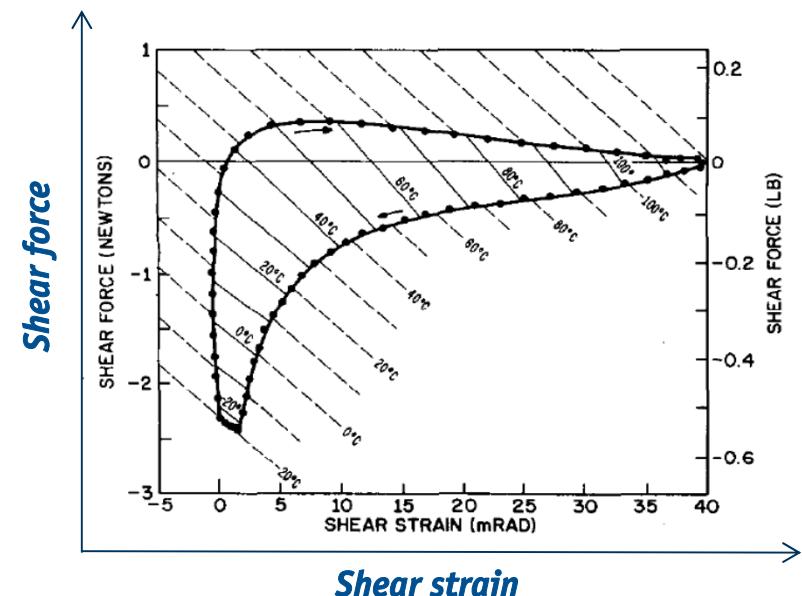
Parameterization of models?



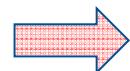
Ref [M. Ciappa et al., "Lifetime Prediction and Design of Reliability Tests for High-Power Devices in Automotive Applications"]

# Stress-Strain Relation for Solder Joint

- How does stress appear and act within materials?
- Correlate stress/strain values with observed failures?
- Hysteresis: stress-strain response of solder joint to periodical temperature cycling



Ref [M. Hall, "Forces, moments, and displacements during thermal chamber cycling of leadless ceramic chip carriers soldered to printed boards"]

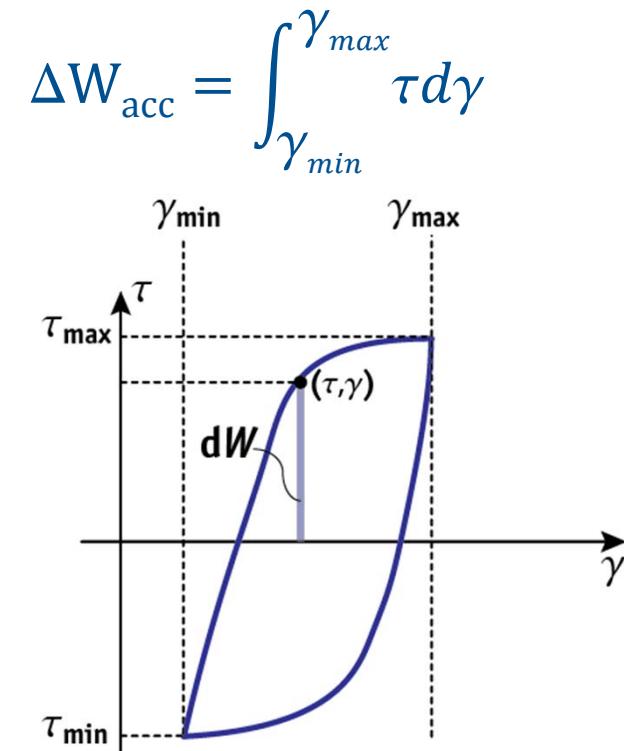


## Energy based models

$$\Delta W_{\text{tot}} = \int_{\gamma_{\min}}^{\gamma_{\max}} \tau d\gamma$$

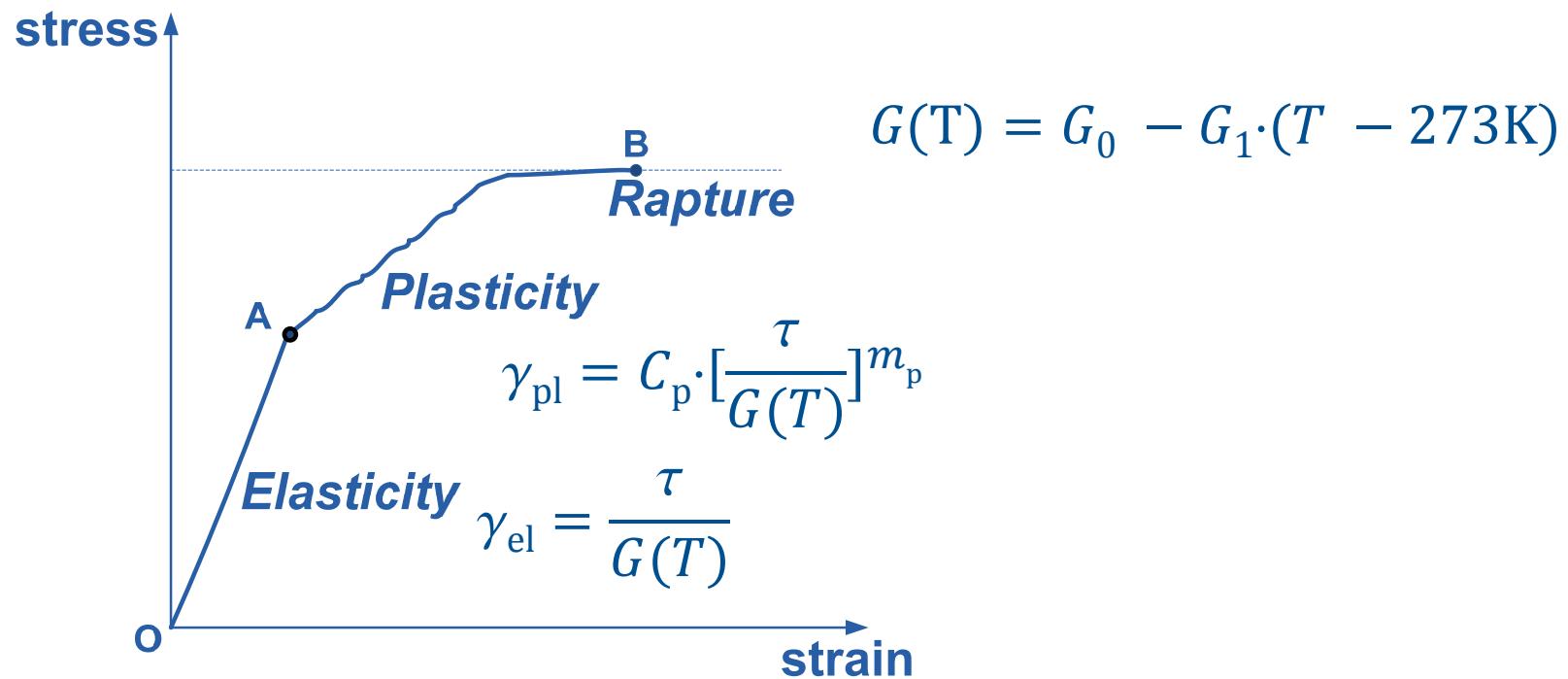
# Proposed Lifetime Modeling Approach

- Main idea of energy-based models
  - \*  $\Delta W_{acc}$ : Total deformation energy accumulated within module
  - \* End-of-Life (EOL): device fails when deformation work  $\Delta W_{acc}$  reaches critical value  $\Delta W_{tot}$
- Clech's algorithm
- Constitutive solder equations



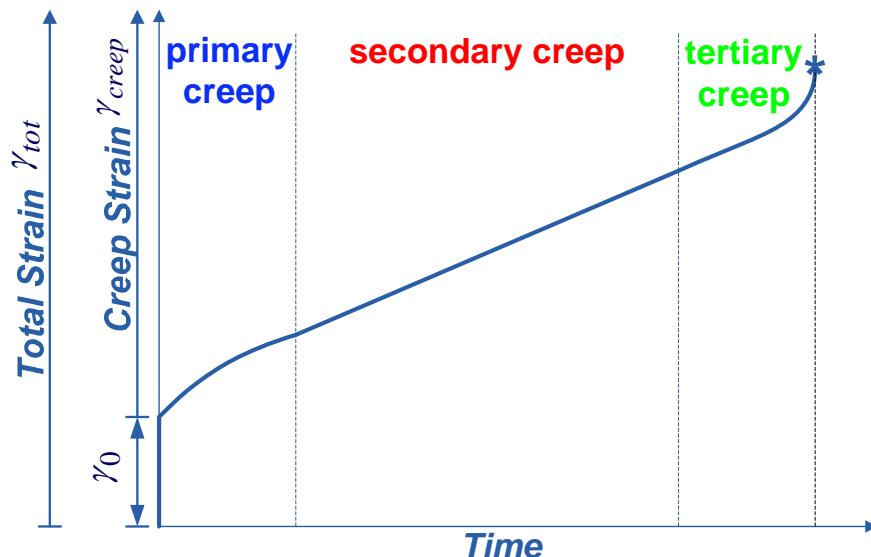
## Solder Physics – Equations (1)

- Fatigue: elastic and plastic time-independent deformation



## Solder Physics – Equations (2)

- Creep: time-dependent plastic deformation



- Material parameters (alloy-dependent)

$$\dot{\gamma}_S = \frac{d\gamma_S}{dt} = B_1 \cdot \frac{G(T)}{T} \cdot \frac{\tau}{G(T)} \cdot e^{-Qb/RT} + B_2 \cdot \frac{G(T)}{T} \cdot \frac{\tau}{G(T)} \cdot e^{-Qm/RT}$$

$$\dot{\gamma}_S = \frac{d\gamma_S}{dt} = C_l \frac{G(T)}{T} [\sinh \frac{\alpha \cdot \tau}{G(T)}]^{n_l} \cdot e^{-Ql/RT} + C_h \frac{G(T)}{T} [\sinh \frac{\alpha \cdot \tau}{G(T)}]^{n_h} \cdot e^{-Qh/RT}$$

$$\dot{\gamma}_S = \frac{d\gamma_S}{dt} = C_1 \frac{G(T)}{T} [\sinh \frac{\alpha \cdot \tau}{G(T)}]^{n_l} \cdot e^{-Q/RT}$$

$$\dot{\gamma}_S = \frac{d\gamma_S}{dt} = A_1 \cdot \tau^{m_1} \cdot e^{-Qa_1/kT \cdot (1 - \tau/\sigma_{01})} + A_2 \cdot \tau^{m_2} \cdot e^{-Qa_2/kT \cdot (1 - \tau/\sigma_{02})}$$

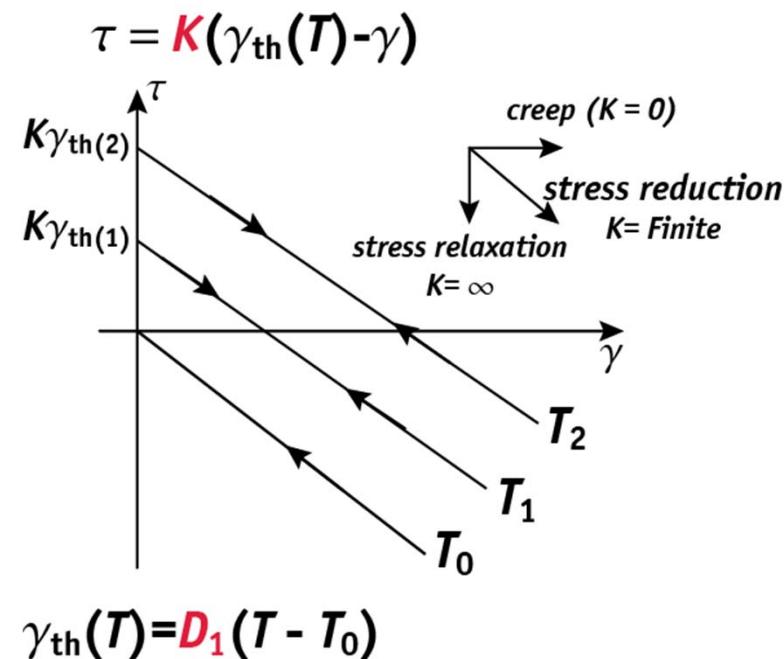
Sn3.5Ag

$$\gamma_T = \gamma_t \cdot \frac{\tau}{G(T)} \cdot (1 - B \cdot \dot{\gamma}_S \cdot t)$$

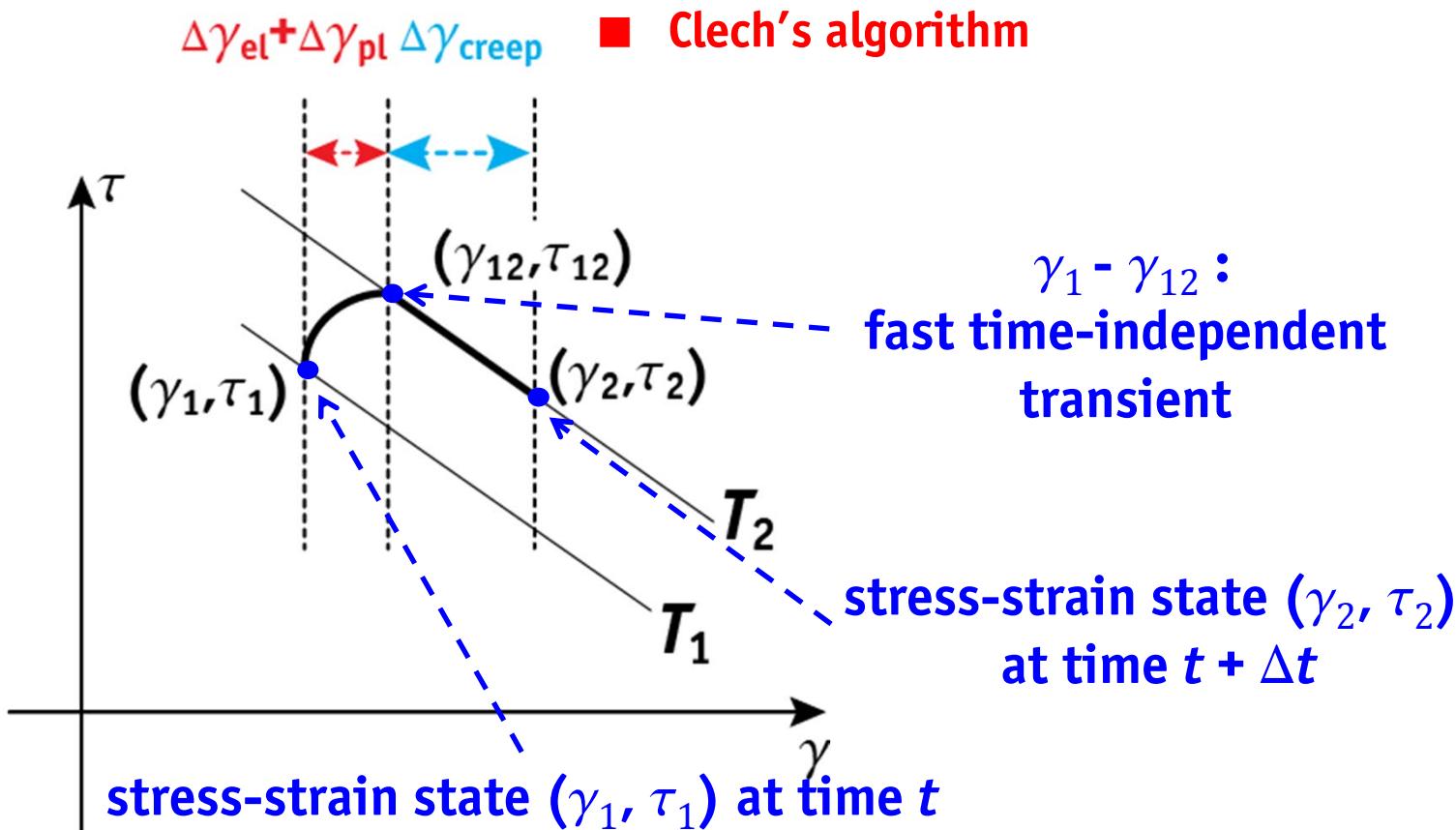
## Stress-Reduction Lines of Solder Material

- Solder geometry properties: height- $h$ , length- $L$ , area- $A$  of solder joint
- Geometry dependent parameters which has to be found:
  - Mechanical modeling of power module based on Finite Element Analysis
  - Optimization Approach

$$\gamma_{shear} + \frac{\tau_{shear}}{K} = D_1 \cdot (T - T_0)$$
$$K \approx \frac{h}{A}, D_1 \approx L \left( \frac{1}{CTE_1} - \frac{1}{CTE_2} \right)$$



## Numerical Modeling of Stress-Strain



# Lifetime Model Parameterization

## ■ Input: 3 PC Tests

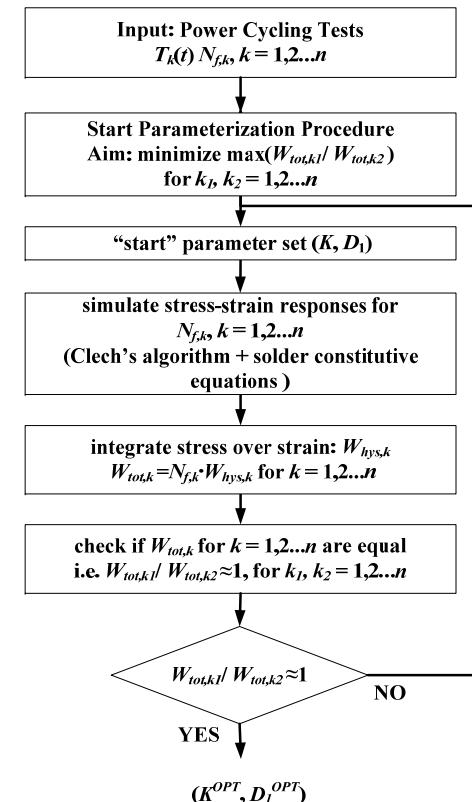
$$(T_1(t), N_{f1}), (T_2(t), N_{f2}), (T_3(t), N_{f3})$$

- $W_{totk} = N_{fk}(W_{hysk})^m, k = 1, 2, 3$
- Exponent  $m$  depends on solder material
- Optimization routine is used to find best

set  $(K, D_1)$  :  $r_{ji} = \frac{W_{toti}}{W_{totj}} \approx 1$

## ■ Relative Lifetime Estimation

$$r = \frac{\int \tau_1 d\gamma_1}{\int \tau_2 d\gamma_2}$$



# Input Data for Lifetime Estimation

## ■ Solder material data from Literature

X. Q. Shi et al., "Creep Behaviour and Deformation Mechanism Map of SnPb Sutectic Solder Alloy," 2003;

J-P. Clech, "An obstacle controlled creep model for SnPb and Sn-based lead-free solders," 2004;

## ■ Power Cycling (PC) Data:

Temperature Profiles -  $T_{\text{solder}}(t)$  & Number of Cycles to Failure -  $N_f$

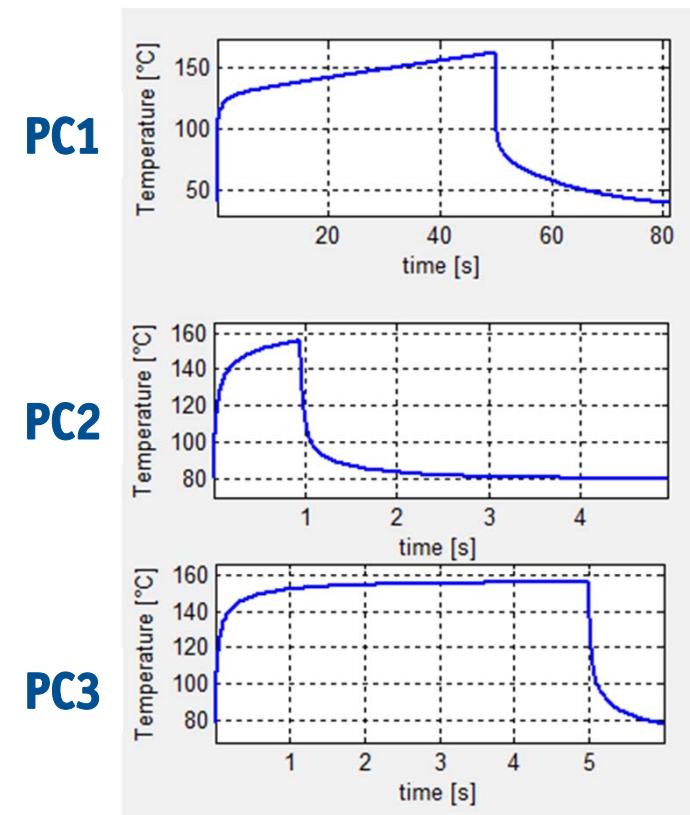
## ■ Solder geometry data:

First task: Parameterization of the proposed lifetime model to determine geometry solder parameters → Searching for optimal parameter set  $[K, D_1]$

Second task: Lifetime estimation for given PC and mission profiles

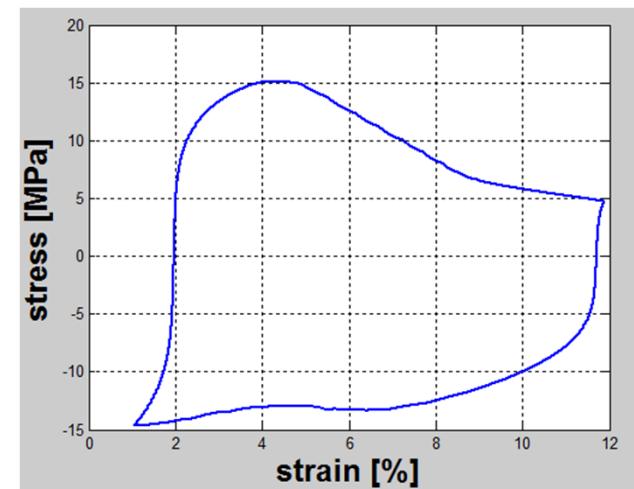
## Verification based on PC Test Data

- PCs with solder (chip solder layer) failure as dominant failure mode
- PC Temperature Profiles:  $T_{\text{solder}}(t)$  extracted based on thermal model of power module
- $[K, D_1]$  selected based on min parameterization error  
(for  $m = 2.2$ ,  $W_{\text{totk}} = N_{\text{fk}}(W_{\text{hysk}})^m$ )
- PC 1-3 used for parameterization:  
PC1:  $\Delta T = 115 \text{ K}$ ,  $T_{\text{max}} = 155^\circ\text{C}$ ,  $t_{\text{on}} = 50\text{s}$   
PC2:  $\Delta T = 70 \text{ K}$ ,  $T_{\text{max}} = 150^\circ\text{C}$ ,  $t_{\text{on}} = 0.95\text{s}$   
PC3:  $\Delta T = 70 \text{ K}$ ,  $T_{\text{max}} = 150^\circ\text{C}$ ,  $t_{\text{on}} = 5\text{s}$



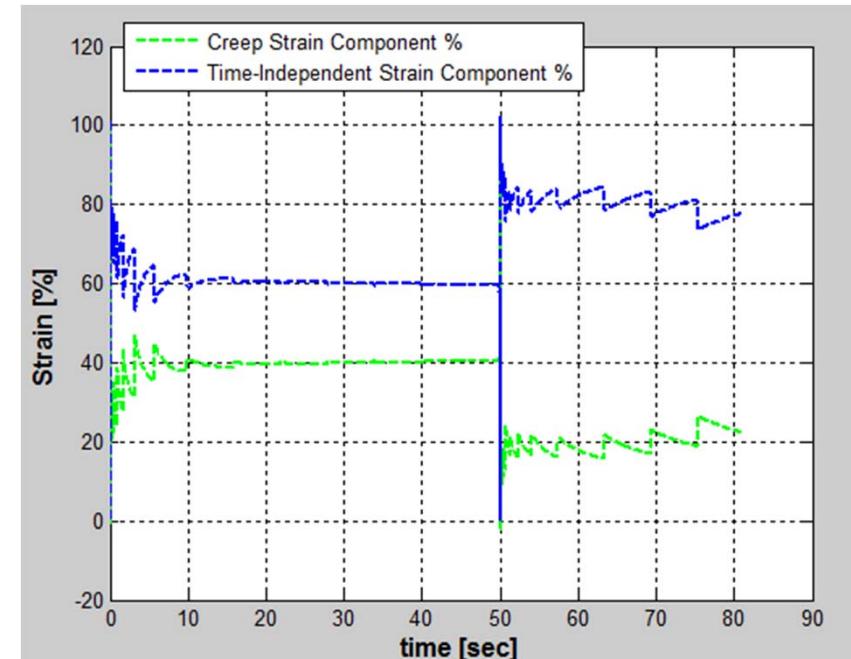
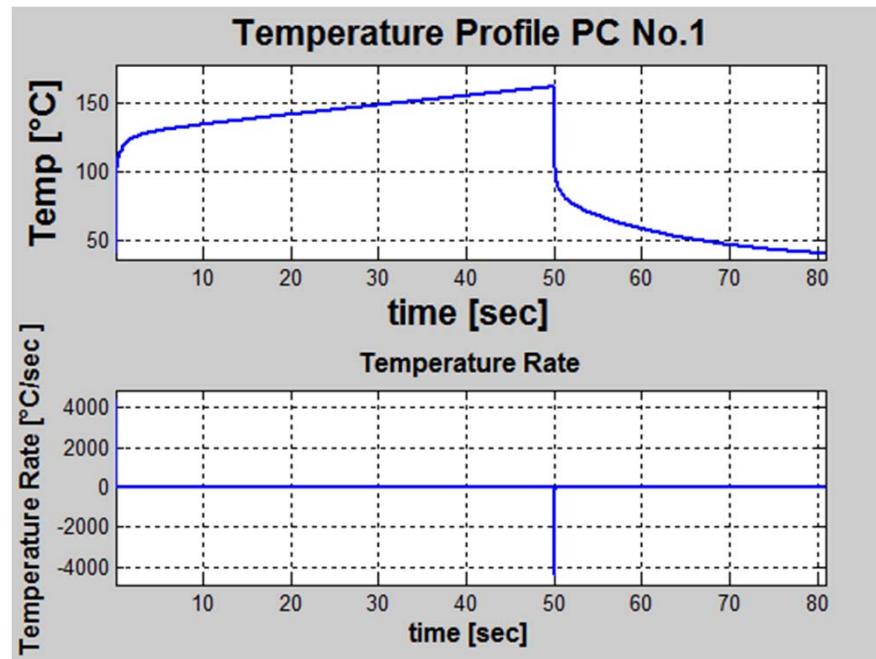
## Results for PC1-3

- Error of parameterization = 1.71  
 $W_{\text{tot1}}, W_{\text{tot2}}, W_{\text{tot3}} \rightarrow (N_{\text{fmin}}, N_{\text{fmax}})$
- $N_{\text{f1}} = 31\ 332,$   
 $N_{\text{fcalc1}} = (31\ 302, 38\ 762, 53654)$
  
- $N_{\text{f2}} = 220\ 279$   
 $N_{\text{fcalc2}} = (128\ 514, 159\ 142, 220\ 279)$
  
- $N_{\text{f3}} = 168\ 390,$   
 $N_{\text{fcalc3}} = (168\ 390, 208\ 521, 288\ 627)$



## Results for PC1-3

### ■ Strain deformation under given $T(t)$



## Lifetime Estimation based on PC1-3

### ■ Verification for PC A-E

PCA:  $\Delta T = 134 \text{ K}$ ,  $T_{\max} = 174^\circ\text{C}$ ,  $t_{\text{on}} = 64.5\text{s}$

$N_{fA} = 28\ 780$ ,  $(23\ 216 - 28\ 749 - 39\ 793) \delta_{\max} = -19\%$

PCB:  $\Delta T = 67 \text{ K}$ ,  $T_{\max} = 146^\circ\text{C}$ ,  $t_{\text{on}} = 0.95\text{s}$

$N_{fB} = 248\ 710$ ,  $(140\ 949 - 174\ 541 - 241\ 594) \delta_{\max} = -0.3\%$

PCC:  $\Delta T = 70 \text{ K}$ ,  $T_{\max} = 150^\circ\text{C}$ ,  $t_{\text{on}} = 1.2\text{s}$

$N_{fC} = 234\ 632$ ,  $(122\ 054 - 151\ 142 - 209\ 205) \delta_{\max} = -10.8\%$

PCD:  $\Delta T = 73 \text{ K}$ ,  $T_{\max} = 150^\circ\text{C}$ ,  $t_{\text{on}} = 2.9\text{s}$

$N_{fD} = 149\ 125$ ,  $(164\ 966 - 204\ 281 - 282\ 758) \delta_{\max} = -9.6\%$

PCE:  $\Delta T = 109 \text{ K}$ ,  $T_{\max} = 148^\circ\text{C}$ ,  $t_{\text{on}} = 13.6\text{s}$

$N_{fE} = 38\ 441$ ,  $(31\ 393 - 38\ 875 - 53\ 809) \delta_{\max} = -18.3\%$

PCX:  $\Delta T = 136 \text{ K}$ ,  $T_{\max} = 176^\circ\text{C}$ ,  $t_{\text{on}} = 2\text{s}$

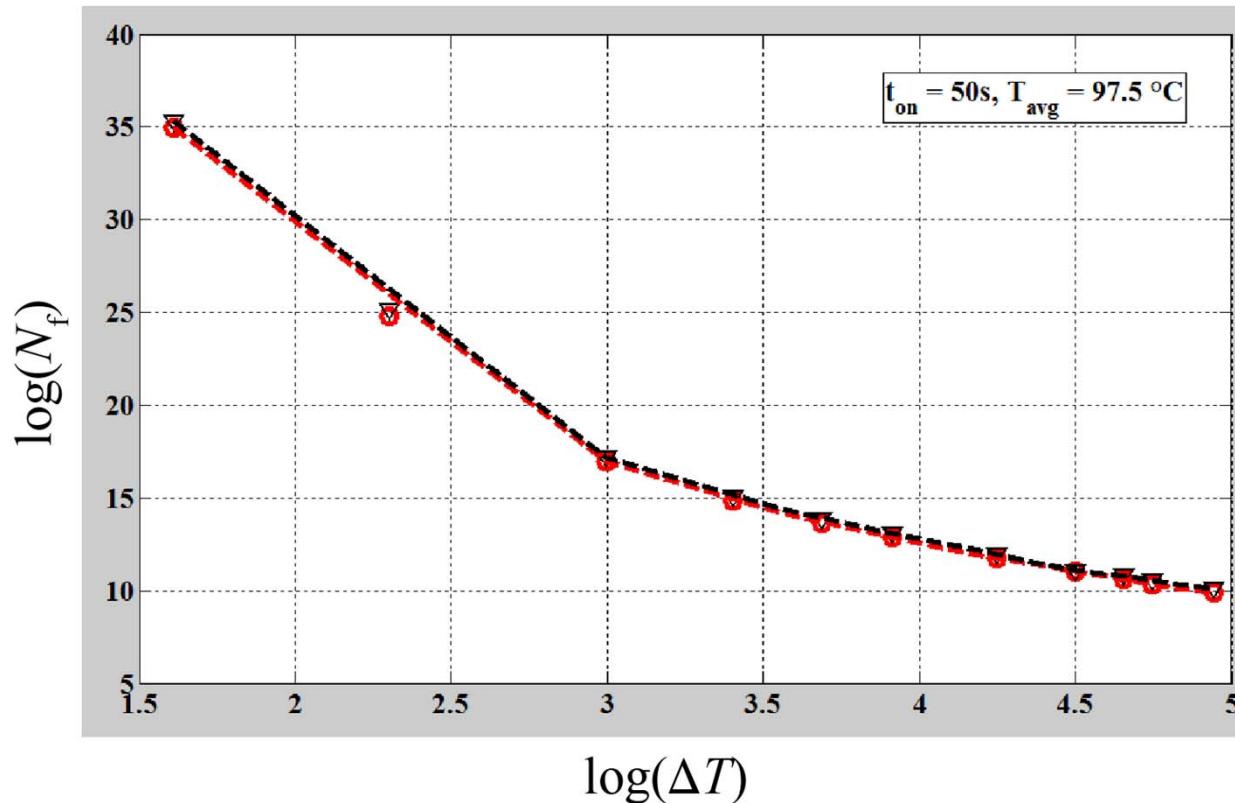
$N_{fx} = 21\ 956$ ,  $(21\ 853 - 27\ 061 - 37\ 457) \delta_{\max} = -23.5\%$

■ Fast or slow temperature rate during  $T_{\max}$  level determine strain development

■ Longer pulse: stationary situation is reached, more deformation

■ Parameter  $\Delta T$  influence lifetime

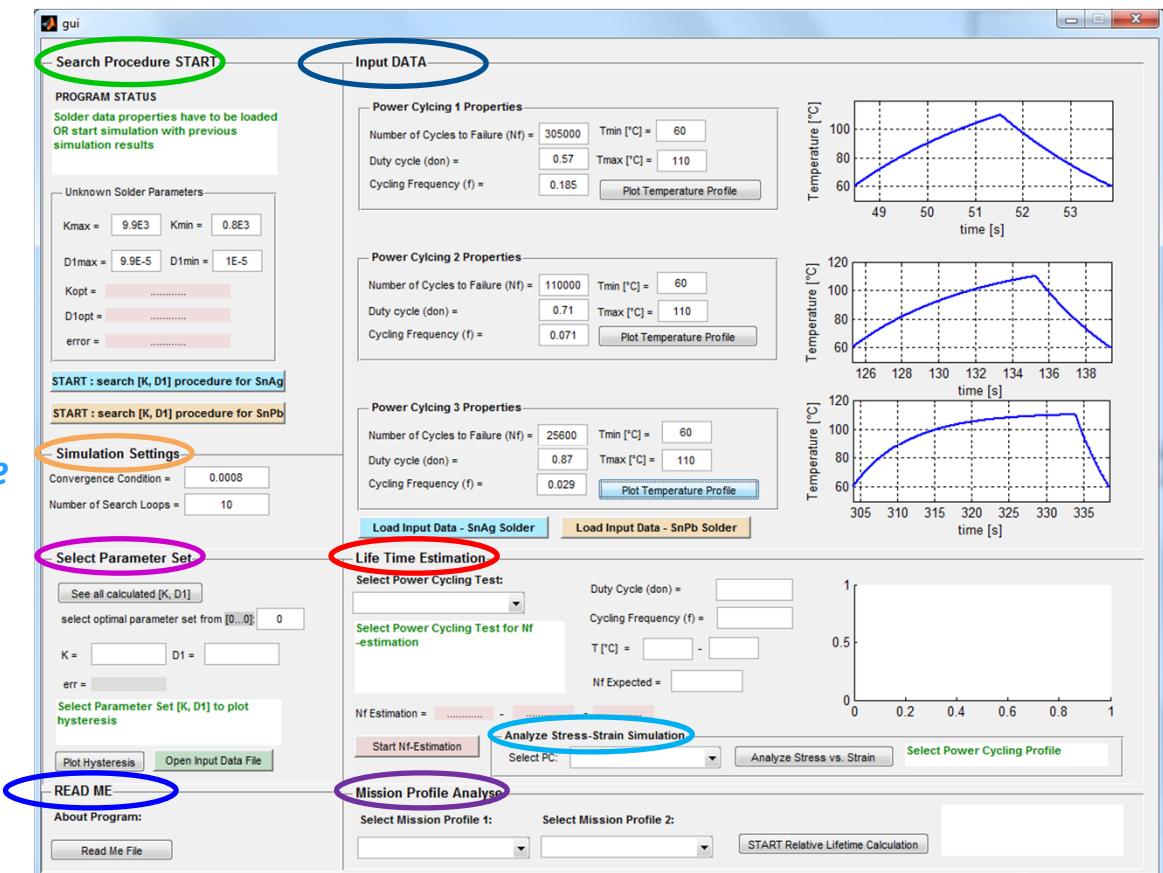
## $N_f$ vs. $\Delta T$ Curves



# MATLAB Graphical User Interface

## MATLAB GUI Options

- *Search Parameters Procedure*
- *Load Input Data*
- *Set Simulation Settings*
- *Modeling for selected [K, D<sub>1</sub>]*
- *PC Lifetime Estimation*
- *Analyze Stress-Strain Response*
- *Rel. Lifetime Calculation*
- *Readme File*



# Thank You !

