

Optimal Design of Inductive Components Based on Accurate Loss and Thermal Models

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Introduction





Introduction

Application of Inductive Components (1) : Buck Converter (DC Current + HF Ripple)

Schematic



Modeling Difficulties

- Non-sinusoidal current / flux waveform
- Current / flux is DC biased

Current / Flux Waveform



Solutions

- FFT of current waveform for the calculation of winding losses
- Determine core loss energy for each segment and for each corner point in the piecewise-linear flux waveform
- Loss Map enables to consider a DC bias





Introduction Application of Inductive Components (2) : Inductor of DAB Converter (Non-Sinusoidal AC Current)



Schematic

Current / Flux Waveform



Modeling Difficulties

- Non-sinusoidal current / flux waveform
- Core losses occur in the interval of constant flux

Solutions

- FFT of current waveform for the calculation of winding losses
- Improved core loss equation that considers relaxation effects





Introduction Application of Inductive Components (3) : Three-Phase PFC (Sinusoidal Current + HF Ripple)

Schematic



Modeling Difficulties

- Non-sinusoidal current / flux waveform
- Major loop and many (DC biased) minor loops

Current / Flux Waveform



Solutions

- FFT of current waveform for the calculation of winding losses
- Determine core loss energy for each segment and for each corner point in the piecewise-linear flux waveform (-> minor loop losses)
- Add major loop losses



Introduction Overview About Different Flux Waveforms







Introduction







Introduction Overview About Other Modeling Issues







Introduction Wide Range of Realization Options

Inductors / Transformers



www.wagnergrimm.ch, www.ferroxcube.com

Core Shapes



www.ferroxcube.com

Conductor Shapes



www.pack-feindraehte.de, www.jiricek.de



Introduction Modeling Inductive Components (1)

Procedure

1) A reluctance model is introduced to describe the electric / magnetic interface, i.e. L = f(i).





Reluctance Model







Introduction Modeling Inductive Components (2)

The following effects will be taken into consideration:

Magnetic Circuit Model (e.g. for Inductance Calculation):

Air gap stray field Non-linearity of core material

Core Losses:

DC Bias

Different flux waveforms (link to circuit simulator) Wide range of flux densities and frequencies Different core shapes



Skin and proximity effect Stray field proximity effect Effect of core on magnetic field distribution Litz, solid, and foil conductors







Introduction







Introduction Motivation for an Accurate Loss Modeling : Multi-Objective Optimization (1)

PFC Rectifier with Input LCL filter



Filter Losses vs. Filter Volume



Converter Losses vs. Converter Volume



Converter = Cooling System + Switches

→ Sometime there are parameters that bring advantages for one subsystem while deteriorating another subsystem (e.g. frequency in above example).





Introduction Motivation for an Accurate Loss Modeling : Multi-Objective Optimization (2)

Losses of a Loss-Optimized Design



- → In order to get an optimal system design, an overall system optimization has to be performed.
- → It is (often) not enough to optimize subsystems independent of each other.



Introduction Motivation for an Accurate Loss Modeling : Multi-Objective Optimization (3)

PFC Rectifier with Input LCL filter



Limits concerning mains

- Tolerable mains harmonics.
- Max. admissible VAr consumption.

Limits concerning filter structure

- Max. admissible volume
- Max. admissible losses

Limits concerning rectifier

- Max. admissible T_{i,max}
- Max. cooling system vol. V_{CS,max}

Optimize for

- Overall PFC rectifier volume
- Overall PFC rectifier losses
- (PFC system cost)





Outline

- Magnetic Circuit Modeling
- Core Loss Modeling
- Winding Loss Modeling
- Thermal Modeling
- Multi-Objective Optimization
- Summary & Conclusion







Magnetic Circuit Modeling Reluctance Model



Electric Network

Magnetic Network

Conductivity / Permeability	К	μ
Resistance / Reluctance	$R = l / (\kappa A)$	$R_{\rm m} = l / (\mu A)$
Voltage / MMF	$V = \int_{P_1}^{P_2} \vec{E} \mathrm{d}\vec{s}$	$V_{\rm m} = \int_{P_1}^{P_2} \vec{H} \mathrm{d}\vec{s}$
Current / Flux	$I = \iint_A \vec{J} \mathrm{d}\vec{A}$	$\Phi = \iint_A \vec{B} \mathrm{d}\vec{A}$







Magnetic Circuit Modeling Why a Reluctance Model is Needed



A reluctance model is needed in order to

calculate the inductance ($L = N^2/R_{tot}$) calculation the saturation current calculate the air gap stray field calculate the core flux density







Magnetic Circuit Modeling Core Reluctance



Reluctance Calculation



Core Reluctance Dimensions









Magnetic Circuit Modeling Air Gap Reluctance : Different Approaches (1)



Assumption of Homogeneous Field Distribution

$$R_{\rm m} = \frac{l_{\rm g}}{\mu_0 A_{\rm g}}$$

 $l_{\rm g}$ Air gap length $A_{\rm g}$ Air gap cross-sectional area

Increase of the Air Gap Cross-Sectional Area

e.g. [1] (for a cross section with dimension *a* x *t*):

$$R_{\rm m} = \frac{l_{\rm g}}{\mu_0 (a + l_{\rm g})(t + l_{\rm g})}$$

 [1] N. Mohan, T. M. Undeland, and W. P. Robbins - "Power Electronics – Converter, Applications, and Design", John Wiley & Sons, Inc., 2003







Magnetic Circuit Modeling Air Gap Reluctance : Different Approaches (2)

Schwarz-Christoffel Transformation



[2] K. J. Binns, P. J. Lawrenson, and C. W. Trowbridge, «The Analytical and Numerical Solution of Electric and Magnetic Fields», John Wiley & Sons, Inc., 1992



Magnetic Circuit Modeling Air Gap Reluctance : Different Approaches (3)

Solution to 2-D problems found in literature, e.g. in [3]

Can't be directly applied to 3-D problems.

Some 3-D solution to problem found in literature; however, they are **complex** [4] and/or limited to one air gape shape [5]

More simple and universal model desired.

- [3] A. Balakrishnan, W. T. Joines, and T. G. Wilson "Air-gap reluctance and inductance calculations for magnetic circuits using a Schwarz-Christoffel transformation", IEEE Transaction on Power Electronics, vol. 12, pp. 654—663, July 1997.
- [4] P. Wallmeier, "Automatisierte Optimierung von induktiven Bauelementen für Stromrichteranwendungen", PhD Thesis, Universität – Gesamthochschule Paderborn, 2001.
- [5] E. C. Snelling, "Soft Ferrites Properties and Applications", 2nd edition, Butterworths, 1988





Magnetic Circuit Modeling Aim of New Model

Air gap reluctance calculation that

- considers the three dimensionality,
- is reasonable easy-to-handle,
- is capable of modeling different shapes of air gaps,
- while still achieving a high accuracy.

Illustration of Different Air Gap Shapes:









Magnetic Circuit Modeling New Model (1)

Basic Structure for the Air Gap Calculation (2-D) [3]



$$R'_{\text{basic}} = \frac{1}{\mu_0 \left[\frac{w}{2l} + \frac{2}{\pi} \left(1 + \ln \frac{\pi h}{4l}\right)\right]}$$





Magnetic Circuit Modeling New Model (2)

2-D (1)













Magnetic Circuit Modeling New Model (3)

2-D (2)

Air Gap Type 1



Air Gap Type 2



Air Gap Type 3



Q





Magnetic Circuit Modeling New Model (4)

$2D \rightarrow 3D$: Fringing Factor (1)





Magnetic Circuit Modeling New Model (5)

 $2D \rightarrow 3D$: Fringing Factor (2)





3-D Fringing Factor:









Magnetic Circuit Modeling FEM Results

3-D FEM Simulation

Modeled Example



Results



a = 40 mm; *h* = 40 mm



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Magnetic Circuit Modeling Experimental Results

Inductance Calculation EPCOS E55/28/21, *N* = 80



TABLE IMeasurement Results of E-Core

Air Gap Length	Calculated	Calculated with	Measured
$l_{ m g}$	classically (3)	new approach (12)	
$1.0\mathrm{mm}$	$1.42\mathrm{mH}$	$1.97\mathrm{mH}$	$2.07\mathrm{mH}$
$1.5\mathrm{mm}$	$0.96\mathrm{mH}$	$1.47\mathrm{mH}$	$1.58\mathrm{mH}$
$2.0\mathrm{mm}$	$0.72\mathrm{mH}$	$1.22\mathrm{mH}$	$1.26\mathrm{mH}$

Saturation Calculation

EPCOS E55/28/21, N = 80, $I_{g} = 1 \text{ mm}, B_{sat} = 0.45 \text{ T}$



TABLE II Measurement Results of E-Core

	Calculated	Calculated with
	classically (3)	new approach (12)
L	$2.75\mathrm{mH}$	$3.55\mathrm{mH}$
$I_{\rm sat}$	4.6 A	3.6 A

Measurement





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 $\emptyset = f(R_{\rm m}(\emptyset), I)$

Magnetic Circuit Modeling

Non-Linearity of the Core Material

This equation must be solved iteratively by using a numerical solving method, e.g. the Newton's method.

Reluctance Model

$R_{m} = f(\emptyset) \quad \emptyset = f(R_{m}(\emptyset), I) = f(\emptyset, I)$

Inductance Calculation

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Schematic



Aim Design PFC rectifier system. Show trade-off between losses and volume. Illustrative example.

Modeling of boost inductors (three individual inductors $L_{2a} = L_{2b} = L_{2c}$) will be step-by-step illustrated in the course of this presentation.

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Example Reluctance Model (1)

Photo & Dimensions





Material Grain-oriented steel (M165-35S) **Power Electronic Systems** Laboratory



Reluctance Model



Calculation of Core Reluctances

$$R_{c1} = \frac{do - 2a}{\mu_0 \mu_r at} + 2 \frac{\frac{\pi}{8}(2a)}{\mu_0 \mu_r t \frac{(2a)}{2}}$$

$$= \frac{60\,\mathrm{m\,m} - 2 \cdot 20\,\mathrm{m\,m}}{\mu_0 \cdot 20\,'000 \cdot 20\,\mathrm{m\,m} \cdot 28\,\mathrm{m\,m}} + 2\frac{\frac{\pi}{8}(2 \cdot 20\,\mathrm{m\,m})}{\mu_0 \cdot 20\,'000 \cdot 28\,\mathrm{m\,m}\,\frac{(2 \cdot 20\,\mathrm{m\,m})}{2}} = 3654\,\frac{\mathrm{A}}{\mathrm{V\,s}}$$

$$R_{c2} = \frac{do - 2a + 2b}{\mu_0 \mu_r at} + 2 \frac{\frac{\pi}{8}(2a)}{\mu_0 \mu_r t \frac{(2a)}{2}}$$

$$\frac{60\,\mathrm{mm} - 2 \cdot 20\,\mathrm{mm} + 2 \cdot\mathrm{h}}{\mu_0 \cdot 20\,'000 \cdot 20\,\mathrm{mm} \cdot 28\,\mathrm{mm}} + 2\,\frac{\frac{\pi}{8}(2 \cdot 20\,\mathrm{mm})}{\mu_0 \cdot 20\,'000 \cdot 28\,\mathrm{mm}\,\frac{(2 \cdot 20\,\mathrm{mm})}{2}} = 12184\,\frac{\mathrm{A}}{\mathrm{Vs}}$$

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Example **Reluctance Model (2)**



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Outline

- Magnetic Circuit Modeling
- Core Loss Modeling
- Winding Loss Modeling
- Thermal Modeling
- Multi-Objective Optimization
- Summary & Conclusion





Core Loss Modeling Overview of Different Core Materials (1)




Core Loss Modeling Overview of Different Core Materials (2)

Selection Criteria

Saturation Flux Density Power Loss Density (Frequency Range) Price etc.

Ferrite

Low Sat. Flux Density (0.45 T) Low Losses Low Price Many Different Shapes Very Brittle

Powder Iron Core

High Sat. Flux Density (1.5 T)
Moderate Losses
Low Price
Many Different Shapes
Distributed Air Gap (low rel. permeability)

Laminated Steel Cores

Very High Sat. Flux Density (2.2T) High Losses Low Price Many Different Shapes

Amorphous Alloys

High Sat. Flux Density (1.5T) Low Losses High Price Limited Available Shapes

Nanocrystalline Materials

High Sat. Flux Density (1.1T) Very Low Losses Very High Price Limited Available Shapes

LF: $B_{\text{SAT}} = B_{\text{max}}$. **HF:** B_{max} is limited by core losses.

Mittwoch, 15. Februar 2012







Core Loss Modeling Overview of Different Core Materials (3)



[7] M. S. Rylko, K. J. Hartnett, J. G. Hayes, M.G. Egan, "Magnetic Material Selection for High Power High Frequency Inductors in DC-DC Converters", in Proc. of the APEC 2009.

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Core Loss Modeling Physical Origin of Core Losses (1)

Weiss Domains / Domain Walls



B-H-Loop



- Spontaneous magnetization.
- Material is divided to saturated domains (Weiss domains).
- In case an external field is applied, the domain walls are shifted or the magnetic moments within the domains change their direction. → The net magnetization becomes greater than zero.
- The flux change is partly irreversible, i.e. energy is dissipated as heat.
- The reason for this are the so called Barkhausen jumps, that lead to local eddy current losses.
- In case the loop is traversed very slowly, these Barkhausen jumps lead to the *static hysteresis losses*.



Core Loss Modeling Physical Origin of Core Losses (2)

B-H-Loop



- If the process would be fully reversible, going from B_1 to B_2 would store potential energy in the magnetic material that is later released (i.e. the area of the closed loop would be zero).
- Since the process is partly irreversible, the area of the closed loop represents the energy loss per cycle

 $W = \oint H \mathrm{d}B$

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Core Loss Modeling Classification of Losses (1)

(Static) hysteresis loss

- Rate-independent *BH* Loop.
- Loss energy per cycle is constant.
- Irreversible changes each within a small region of the lattice (Barkhausen jumps).
- These rapid, irreversible changes are produced by relatively strong local fields within the material.



- Eddy current losses
- Residual Losses Relaxation losses



Core Loss Modeling Classification of Losses (2)

- (Static) hysteresis loss
- Eddy current losses
 - Depend on material conductivity and core shape.
 - Affect *BH* loop.
- Residual Losses Relaxation losses





Core Loss Modeling Classification of Losses (3)

- (Static) hysteresis loss
- Eddy current losses
- Residual losses Relaxation losses
 - Rate-dependent *BH* Loop.
 - Reestablishment of a thermal equilibrium is governed by relaxation processes.
 - Restricted domain wall motion.



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Core Loss Modeling Typical Flux Waveforms









Core Loss Modeling Outline of Different Modeling Approaches

Steinmetz Approach

$$P = k f^{\alpha} B^{\beta}$$

- Simple
- Steinmetz parameter are valid only in a limited flux density and frequency range
- DC Bias not considered
- (Only for sinusoidal flux waveforms)

Loss Separation

$$P = P_{\rm hyst} + P_{\rm eddy} + P_{\rm residual}$$

- Needed parameters often unknown
- Model is widely applicable
- Increases physical understanding of loss mechanisms

Relative core losses versus frequency (measured on R16 toroids)



Loss Map Approach

(Loss Database)

 Measuring core losses is indispensable to overcome limits of Steinmetz approach

Hysteresis Model

(e.g. Preisach Model, Jiles-Atherton Model)

- Difficult to parameterize
- Increases physical understanding of loss mechanisms





Core Loss Modeling Overview of Hybrid Modeling Approach

"The best of both worlds" (Steinmetz & Loss Map approach)



Outline of Discussion

Derivation of the i²GSE. (1)

- How to measure core losses in order to build loss map. (2)
- Use of loss map. (3)
- How to calculate core losses for cores of different shapes? (4)



Core Loss Modeling Derivation of the i²GSE – Motivation (1)

Steinmetz Equation SE

$$P_{\rm v} = k f^{\alpha} \hat{B}^{\beta}$$

- Only sinusoidal waveforms (→ iGSE).
- P_v: time-average power loss per unit volume

iGSE

$$P_{v} = \frac{1}{T} \int_{0}^{T} k_{i} \left| \frac{\mathrm{d}B}{\mathrm{d}t} \right|^{\alpha} \left(\Delta B \right)^{\beta - \alpha} \mathrm{d}t$$
$$k_{i} = \frac{k}{\left(2\pi\right)^{\alpha - 1} \int_{0}^{2\pi} \left| \cos \theta \right|^{\alpha} 2^{\beta - \alpha} \mathrm{d}\theta}$$

- DC bias not considered
- Relaxation effect not considered (\rightarrow i²GSE)
- Steinmetz parameter are valid only for a limited flux density and frequency range



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Core Loss Modeling Derivation of the i²GSE – Motivation (2)

iGSE [8]



How to apply the formula?



[8] K. Venkatachalam, C. R. Sullivan, T. Abdallah, and H. Tacca, "Accurate prediction of ferrite core loss with nonsinusoidal waveforms using only Steinmetz parameters", in Proc. of IEEE Workshop on Computers in Power Electronics, pp. 36-41, 2002.

ldea

- Generalized formula that is applicable for different flux waveforms
- Losses depend on dB/dt

For Sinusoidal Waveforms

$$P_{v} = \frac{1}{T} \int_{0}^{T} k_{i} \left| \frac{\mathrm{d}B}{\mathrm{d}t} \right|^{\alpha} \left(\Delta B \right)^{\beta - \alpha} \mathrm{d}t = k f^{\alpha} \left(\frac{\Delta B}{2} \right)^{\beta}$$





Core Loss Modeling Derivation of the i²GSE – Motivation (3)

Waveform



Results



iGSE

$$P_{v} = \frac{1}{T} \int_{0}^{T} k_{i} \left| \frac{\mathrm{d}B}{\mathrm{d}t} \right|^{\alpha} \left(\Delta B \right)^{\beta - \alpha} \mathrm{d}t$$

Conclusion

Losses in the phase of constant flux!





Core Loss Modeling Derivation of the i²GSE – *B*-*H*-Loop



Relaxation Losses

- Rate-dependent *BH* Loop.
- Reestablishment of a thermal equilibrium is governed by relaxation processes.
- Restricted domain wall motion.



Current Waveform





Core Loss Modeling Derivation of the i²GSE – Model Derivation 1 (1)

Waveform



Loss Energy per Cycle



Relaxation loss energy can be described with





au is independent of operating point.

How to determine ΔE ?





Core Loss Modeling Derivation of the i²GSE – Model Derivation 1 (2)

ΔE – Measurements





Waveform







 $\Delta E = k_{\rm r} \left| \frac{\rm d}{{\rm d}t} B(t) \right|^{\alpha_{\rm r}} (\Delta B)^{\beta_{\rm r}}$







Core Loss Modeling Derivation of the i²GSE – Model Derivation 1 (3)



Model Part 1

$$P_{\rm v} = \frac{1}{T} \int_{0}^{T} k_i \left| \frac{\mathrm{d}B}{\mathrm{d}t} \right|^{\alpha} (\Delta B)^{\beta - \alpha} \mathrm{d}t + \sum_{l=1}^{n} P_{\rm rl}$$

$$P_{\rm rl} = \frac{1}{T} k_{\rm r} \left| \frac{\rm d}{{\rm d}t} B(t) \right|^{\alpha_{\rm r}} (\Delta B)^{\beta_{\rm r}} \left(1 - {\rm e}^{-\frac{t_{\rm l}}{\tau}} \right)$$



Core Loss Modeling Derivation of the i²GSE – Model Derivation 2 (1)

Waveform







Explanation

- 1) For values of *D* close to 0 or close to 1 a loss underestimation is expected when calculating losses with iGSE (no relaxation losses included).
- 2) For values of *D* close to 0.5 the iGSE is expected to be accurate.
- 3) Adding the relaxation term leads to the upper loss limit, while the iGSE represents the lower loss limit.
- 4) Losses are expected to be in between the two limits, as has been confirmed with measurements.



Core Loss Modeling Derivation of the i²GSE – Model Derivation 2 (2)

Waveform





Power Loss



$$P_{\rm v} = \frac{1}{T} \int_{0}^{T} k_{i} \left| \frac{\mathrm{d}B}{\mathrm{d}t} \right|^{\alpha} \left(\Delta B \right)^{\beta - \alpha} \mathrm{d}t + \sum_{l=1}^{n} \mathbf{Q}_{\rm rl} P_{\rm rl}$$

 $Q_{r/}$ should be 1 for D = 0

 $Q_{r/}$ should be 0 for D = 0.5

 $Q_{\rm r/}$ should be such that calculation fits a triangular waveform measurement.

$$Q_{\mathrm{r}l} = \mathrm{e}^{-q_{\mathrm{r}} \left| \frac{\mathrm{d}B(t+)/\mathrm{d}t}{\mathrm{d}B(t-)/\mathrm{d}t} \right|} \left(= \mathrm{e}^{-q_{\mathrm{r}} \frac{D}{1-D}} \right)$$





Core Loss Modeling Derivation of the i²GSE – Model Derivation 2 (3)

Waveform









Core Loss Modeling Derivation of the i²GSE – Summary

The improved-improved Generalized Steinmetz Equation (i²GSE) [9]

$$P_{\rm v} = \frac{1}{T} \int_{0}^{T} k_i \left| \frac{\mathrm{d}B}{\mathrm{d}t} \right|^{\alpha} \left(\Delta B \right)^{\beta - \alpha} \mathrm{d}t + \sum_{l=1}^{n} Q_{\rm rl} P_{\rm rl}$$

with

$$P_{\mathrm{r}l} = \frac{1}{T} k_{\mathrm{r}} \left| \frac{\mathrm{d}}{\mathrm{d}t} B(t) \right|^{\alpha_{\mathrm{r}}} (\Delta B)^{\beta_{\mathrm{r}}} \left(1 - \mathrm{e}^{-\frac{t_{\mathrm{l}}}{\tau}} \right)$$



and

$$Q_{\rm rl} = {\rm e}^{-q_{\rm r} \left| \frac{{\rm d}B(t+)/{\rm d}t}{{\rm d}B(t-)/{\rm d}t} \right|}$$

[9] J. Mühlethaler, J. Biela, J.W. Kolar, and A. Ecklebe, "Improved Core Loss Calculation for Magnetic Components Employed in Power Electronic Systems", in Proc. of the APEC, Ft. Worth, TX, USA, 2011.





Core Loss Modeling Derivation of the i²GSE – Example







Core Loss Modeling Derivation of the i²GSE – Conclusion



Steinmetz parameter are valid only in a limited flux density and frequency range.

Core Losses vary under DC bias condition.

Modeling relaxation and DC bias effects need parameters that are not given by core material manufacturers.



Measuring core losses is indispensable!





Core Loss Modeling Overview of Hybrid Modeling Approach

"The best of both worlds" (Steinmetz & Loss Map approach)







Core Loss Modeling Core Loss Measurement – Measurement Principle







 Voltage
 0 ... 450 V

 Current
 0 ... 25 A

 Frequency
 0 ... 200 kHz

Schematic



Loss Extraction









Core Loss Modeling Core Loss Measurement - Overview







Core Loss Modeling Overview of Hybrid Modeling Approach

"The best of both worlds" (Steinmetz & Loss Map approach)



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Core Loss Modeling Needed Loss Map Structure

Typical flux waveform

MMM (1)

Content of Loss Map

Relaxation

B-H-Relation















Core Loss Modeling Minor and Major Loops







Core Loss Modeling Hybrid Loss Modeling Approach (1)







Core Loss Modeling Hybrid Loss Modeling Approach (2)

Evaluated for the according corner point in a piecewise-linear flux waveform. $\$







Core Loss Modeling

Hybrid Loss Modeling Approach (3)

Interpolation and Extrapolation

 $(H_{\rm DC}^{*}, T^{*}, \Delta B^{*}, f^{*})$





Core Loss Modeling Hybrid Loss Modeling Approach (4)

Advantages of Hybrid Approach (Loss Map and i²GSE):

Relaxation effects are considered (i²GSE).

A good interpolation and extrapolation between premeasured operating points is achieved.

Loss map provides accurate i²GSE parameters for a wide frequency and flux density range.

A DC bias is considered as the loss map stores premeasured operating points at different DC bias levels.





Core Losses Summary of Loss Density Calculation







Core Loss Modeling Overview of Hybrid Modeling Approach

"The best of both worlds" (Steinmetz & Loss Map approach)







Core Loss Modeling Effect of Core Shape

Procedure

- 1) The flux density in every core section of (approximately) homogenous flux density is calculated.
- 2) The losses of each section are calculated.
- The core losses of each section are then summed-up to obtain the total core losses.

Reluctance Model






Core Loss Modeling Effective Core Dimensions of Toroid

Motivation for Effective Core Dimensions

Core loss *densities* are needed to model core losses. It is difficult to determine these loss densities from a toroid, since the flux density is not distributed homogeneously in a toroid.

Definition: Ideal Toroid

A toroid is ideal when he has a homogenous flux density distribution over the radius $(r_1 \cong r_2)$.

Idea for Real Toroid

Find effective core magnetic length and cross section, so one can calculate as if it were an ideal toroid, i.e. as if the flux density distribution were homogenous.

Effective magnetic length

$$l_{\rm e} = \frac{2\pi \ln r_2 / r_1}{1 / r_1 - 1 / r_2}$$

Effective magnetic cross-section

$$A_{\rm e} = \frac{h \ln^2 r_2 / r_1}{1 / r_1 - 1 / r_2}$$







Core Loss Modeling Impact of Core Shape on Eddy Current Losses

Eddy current loss density can be determined as [5]

$(\pi \hat{R}fd)^2$	Geometry	$k_{ m ec}$
$P_{\rm eddy} = \frac{(\pi D J \mu)}{2}$	laminations of thickness d	6
$k_{\rm ec}\rho$	cylinder of diameter d	16
	sphere of diameter d	20

For a laminated core it is



- → The eddy current losses per unit volume depend not on the shape of the bulk material, but on the size and geometry of the insulated regions.
- → In case of laminated iron cores, it is still appropriate to calculate with core loss densities that have been measured on a sample core with a geometrically different bulk material, but with the same lamination or tape thickness.
- [5] E. C. Snelling, "Soft Ferrites Properties and Applications", 2nd edition, Butterworths, 1988







Core Loss Modeling Effect in Tape Wound Cores



www.vacuumschmelze.de



Thin ribbons (approx. 20 μm)Wound as toroid or as double C core.Amorphous or nanocrystalline materials.

Losses in gapped tape wound cores higher than expected!







Core Loss Modeling Effect in Tape Wound Cores - Cause 1 : Interlamination Short Circuits

Machining process

Surface short circuits introduced by machining (particular a problem in in-house production).



After treatment may reduce this effect. At ETH, a core was put in an 40% ferric chloride FeCl₃ solution after cutting, which substantially (more than 50%) decreased the core losses.





Core Loss Modeling Effect in Tape Wound Cores - Cause 2 : Orthogonal Flux Lines (1)



A flux orthogonal to the ribbons leads to very high eddy current losses!





Core Loss Modeling Effect in Tape Wound Cores - Cause 2 : Orthogonal Flux Lines (2)

An experiment that illustrates well the loss increase due to an orthogonal flux is given here.









Core Loss Modeling Effect in Tape Wound Cores - Cause 2 : Orthogonal Flux Lines (3)

Core loss increase due to leakage flux in transformers.



Measurement Set Up

Results













Core Loss Modeling Effect in Tape Wound Cores - Cause 2 : Orthogonal Flux Lines (4)

In [10] a core loss increase with increasing air gap length has been observed.



Fig.1 Core loss per cycle W/f in FINEMET, Fe-based amorphous, and ferrite cut cores as a function of inverse of the effective permeability μ_{T} .



Fig.2 Schematic representation of in-plane eddy current generated by leakage flux normal to ribbon surfaces.

[10] H. Fukunaga, T. Eguchi, K. Koga, Y. Ohta, and H. Kakehashi, "High Performance Cut Cores Prepared From Crystallized Fe-Based Amorphous Ribbon", in IEEE Transactions on Magnetics, vol. 26, no. 5, 1990.

Figures from [10]

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Example **Core Loss Modeling**

Photo & Dimensions





An approximately homogeneous flux density distribution inside the core.

Reluctance Model





Material Grain-oriented steel (M165-35S)

Flux Density Waveform



MATLAB Presentation







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Outline

- Magnetic Circuit Modeling
- Core Loss Modeling
- Winding Loss Modeling
- Thermal Modeling
- Multi-Objective Optimization
- Summary & Conclusion





Winding Loss Modeling Skin Effect (1)

H-field in conductor

Ampere's Law



 $\oint \mathbf{H} \, d\mathbf{l} = \iint \mathbf{J} \, \mathbf{d} \mathbf{A}$

Faraday's Law

$$\oint \mathbf{E} \, \mathrm{d}\mathbf{l} = -\frac{\mathrm{d}}{\mathrm{d}t} \iint \mathbf{B} \, \mathrm{d}\mathbf{A}$$







Winding Loss Modeling Skin Effect (2)







Winding Loss Modeling Skin Effect (3)

Skin Depth (, where the current density has 1/e of surface value)



Power Loss Increase with Frequency

$$P_{\rm S} = F_{\rm R}(f) \cdot R_{\rm DC} \cdot \hat{I}^2$$

2





Winding Loss Modeling Skin Effect (4)

Current Distributions



Figure from [19]





Winding Loss Modeling Proximity Effect (1)

H-field of neighboring conductor induces eddy currents



Ampere's Law

$$\oint \mathbf{H} \, \mathrm{d} \mathbf{l} = \iint \mathbf{J} \, \mathrm{d} \mathbf{A}$$

Faraday's Law

$$\oint \mathbf{E} \, \mathrm{d}\mathbf{l} = -\frac{\mathrm{d}}{\mathrm{d}t} \iint \mathbf{B} \, \mathrm{d}\mathbf{A}$$





Winding Loss Modeling **Proximity Effect (2)**





Winding Loss Modeling Skin vs. Proximity Effect

Situation

$$(f = 100 \text{ kHz}, I_{\text{peak}} = 1 \text{ A}, H_{\text{e,peak}} = 1000 \text{ A/m})$$



Results



Definition

Skin Effect Losses P_{Skin}

Losses due to current *I*, including loss increase due to self-induced eddy currents.

Proximity Effect Losses P_{Prox}

Losses due to eddy currents induced by external magnetic field $H_{\rm e}$.





Winding Loss Modeling Litz Wire (1) - What are Litz wires?



Advantages of Litz wires

HF losses can be reduced substantially

Disadvantages of Litz wires

High price Heat dissipation difficult

Implementation 7 strands - 22 20 2B - Insulation of litz wire 2E 2G 2F - Strand insulation (2) 20 2B - Strand insulation







Winding Loss Modeling Litz Wire (2) - Why Litz Wires Have to be Twisted? (1)

Bundle-Level Skin Effect







Winding Loss Modeling Litz Wire (3) - Why Litz Wires Have to be Twisted? (2)

Bundle-Level Proximity Effect











Winding Loss Modeling Litz Wire (4) – Strand-Level Effects

Internal and External Fields lead to Internal and External Proximity Effects





Winding Loss Modeling Litz Wire (5) – Types of Eddy-Current Effects in Litz Wire



Figure from [11] Ch. R. Sullivan, "Optimal Choice for Number of Strands in a Litz-Wire Transformer Winding", in IEEE Transactions on Power Electronics, vol. 14, no. 2, 1999.







Winding Loss Modeling Litz Wire (6) – Real Litz Wire



Operating Point f = 20 kHz / n = 130 / $d_{\rm i} = 0.4 \, {\rm mm}$

How do "real" Litz wires behave? [12]

Skin Effect / Internal Proximity Effect

External Proximity Effect

$$R_{\rm skin,\lambda} = \lambda_{\rm skin} R_{\rm skin,ideal} + (1 - \lambda_{\rm skin}) R_{\rm skin,parallel}$$
$$R_{\rm prox,\lambda} = \lambda_{\rm prox} R_{\rm prox,ideal} + (1 - \lambda_{\rm prox}) R_{\rm prox,parallel}$$

7 bundles with 35 strands each¹): Litz Wire Type 1: $\lambda_{\rm skin} \approx 0.5$ / $\lambda_{\rm prox} \approx 0.99$ Litz Wire Type 2: 4 bundles with 61/62 strands each¹): $\lambda_{\rm skin} \approx 0.9$ / $\lambda_{\rm prox} \approx 0.99$

[12] H. Rossmanith, M. Doebroenti, M. Albach, and D. Exner, "Measurement and Characterization of High Frequency Losses in Nonideal Litz Wires", IEEE Transactions on Power Electronics, vol. 26, no. 11, November 2011







Winding Loss Modeling Litz Wire (7) - Are Litz Wires Better than Solid Conductors?







Winding Loss Modeling Foil Windings Enclosed by Magnetic Material



Disadvantages of foil windings

Increased winding capacitance Risk of orthogonal flux "Skin" of foil conductor larger than of round conductor with same cross section; hence, skin effect losses lower in foil conductor.







Winding Loss Modeling Foil Windings Not Enclosed by Magnetic Material (1)

Single Conductor









Orthogonal flux leads to increased skin and proximity effect.





Winding Loss Modeling Foil Windings Not Enclosed by Magnetic Material (2)



(Foil) Windings with Return Conductors





Winding Loss Modeling Overview About Different Winding Types



Table and Figure from [13] M. Albach, "Induktive Komponenten in der Leistungselektronik", VDE Fachtagung - ETG Fachbereich Q1 "Leistungselektronik und Systemintegration", Bad Nauheim, 14.04.2011



Winding Loss Modeling Skin Effect of Foil Conductor

Geometry Considered



Current Distribution



$$P_{\rm S} = F_{\rm F}(f) \cdot R_{\rm DC} \cdot \hat{I}^2$$

(Loss per unit length)

with

$$F_{\rm F} = \frac{v}{4} \frac{\sinh v + \sin v}{\cosh v - \cos v}$$
$$R_{\rm DC} = \frac{1}{\sigma b h}$$
$$v = \frac{h}{\delta}$$
$$\delta = \frac{1}{\sqrt{\pi \mu_0 \sigma f}}$$

F_F evaluated







Winding Loss Modeling Proximity Effect of Foil Conductor

Geometry Considered



Current Distribution



$$P_{\rm P} = G_{\rm F}(f) \cdot R_{\rm DC} \cdot \hat{H}_{\rm S}^2$$

(Loss per unit length)

with











Winding Loss Modeling Skin Effect of Solid Round Conductor



$$P_{\rm S} = F_{\rm R}(f) \cdot R_{\rm DC} \cdot \hat{I}^2$$

(Loss per unit length)

with







Winding Loss Modeling Proximity Effect of Solid Round Conductor

Geometry Considered



$$P_{\rm P} = G_{\rm R}(f) \cdot R_{\rm DC} \cdot \hat{H}_{\rm S}^2$$

(Loss per unit length)

with

$G_{\rm R} \text{ evaluated}$ $R_{\rm DC} = \frac{4}{\sigma \pi d^2}$ $\xi = \frac{d}{\sqrt{2}\delta}$ $\delta = \frac{1}{\sqrt{\pi \mu_0 \sigma f}}$ $G_{\rm R} = -\frac{\xi \pi^2 d^2}{2\sqrt{2}} \left[\frac{\text{ber}_2(\xi) \text{ber}_1(\xi) + \text{ber}_2(\xi) \text{bei}_1(\xi)}{\text{ber}_0(\xi)^2} + \frac{\text{bei}_2(\xi) \text{bei}_1(\xi) - \text{bei}_2(\xi) \text{ber}_1(\xi)}{\text{ber}_0(\xi)^2} + \frac{\text{bei}_2(\xi) \text{bei}_1(\xi) - \text{bei}_2(\xi) \text{ber}_1(\xi)}{\text{ber}_0(\xi)^2} \right]$ (d = 1 m)



 d_i



Winding Loss Modeling Skin and Proximity Effect of Litz Wire



Skin Effect

$$P_{\rm S} = n \cdot R_{\rm DC} \cdot F_{\rm R}(f) \cdot \left(\frac{\hat{I}}{n}\right)^2$$
(Loss per unit length)

Proximity Effect

$$P_{\rm P} = P_{\rm P,e} + P_{\rm P,i}$$

= $n \cdot R_{\rm DC} \cdot G_{\rm R} (f) \cdot \left(H_{\rm e}^2 + \frac{\hat{I}^2}{2\pi^2 d_{\rm a}^2} \right)$

(Loss per unit length)

Average internal field H_i under the assumption of a homogeneous current distribution inside the Litz wire.

Losses in Litz Wires



 $(25 \text{ x } d_i = 0.5 \text{ mm}, I_{\text{peak}} = 5 \text{ A}, H_{\text{e,peak}} = 300 \text{ A/m})$

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Winding Loss Modeling Orthogonality of Winding Losses

It is valid to calculate the losses for each frequency component independently and total them up.

$$P = \sum_{i=0}^{\infty} \left(P_{\mathrm{S},i} + P_{\mathrm{P},i} \right)$$

It is valid to calculate the skin and proximity losses independently and total them up.

[14] J. A. Ferreira, "Improved analytical modeling of conductive losses in magnetic components", in IEEE Transactions on Power Electronics, vol. 9, no. 1, 1994.





Winding Loss Modeling Calculation of External Field H_e (1D - Approach)

Un-Gapped Transformer Cores



$$P = R_{\rm DC} \left(F_{\rm R/F} \hat{I}^2 NM + NG_{\rm R/F} \sum_{m=1}^{M} \hat{H}_{\rm avg,m}^2 \right) l_{\rm m}$$

with

$$H_{\rm avg} = \frac{1}{2} \Big(H_{\rm left} + H_{\rm right} \Big)$$

it is

$$P = R_{\rm DC} \hat{I}^2 \left(F_{\rm R/F} NM + N^3 M G_{\rm R/F} \frac{4M^2 - 1}{12b_{\rm F}^2} \right) l_{\rm m}$$

where

N... the number of conductors per layer (i.e. N = 1 for foil windings)

M... the number of layers.



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Winding Loss Modeling Short Foil Conductors



"Porosity Factor"

$$\eta = \frac{Nb_{\rm L}}{b_{\rm F}}$$

Redefinition of Parameters

$$\sigma' = \eta \sigma$$
$$\delta' = \frac{1}{\sqrt{\pi f \sigma' \mu_0}}$$
$$\nu' = \frac{h}{\delta'}$$






Winding Loss Modeling FEM Simulations : Foil Windings







Winding Loss Modeling Calculation of External Field *H*_e (2D - Approach)

Gapped cores: 2D approach is necessary !









Winding Loss Modeling Effect of the Air Gap Fringing Field

The air gap is replaced by a fictitious current, which ...

... has the value equal to the magneto-motive force (mmf) across the air gap.



 \rightarrow An accurate air gap reluctance model is needed!







Winding Loss Modeling Effect of the Core Material





Winding Loss Modeling Calculation of External Field *H*_e (2D - Approach)

Gapped cores: 2D approach



Winding Arrangement



External field vector across conductor $q_{xi;yk}$

$$\hat{H}_{e} = \left| \sum_{u=1}^{m} \sum_{l=1}^{n} \epsilon(u, l) \frac{\hat{i}_{x_{u}, y_{l}} \left((y_{l} - y_{k}) - j(x_{u} - x_{i}) \right)}{2\pi \left((x_{u} - x_{i})^{2} + (y_{l} - y_{k})^{2} \right)} \right|$$







Winding Loss Modeling Different Winding Sections

Section 2 Section 2 Section 2 Conductor Condu Core Material Core Material Core Material Section 2 Section 2 Phase C Phase A Phase B Section 1 Section 1 Section 2 Section 2 Section 2 Section 1 Section 2 Many mirroring steps Only one mirroring step necessary in order to push necessary (only one wall). the walls away.

Normally, higher proximity losses in Section 1.





Winding Loss Modeling

FEM Simulations : Round Windings (Including Litz Wire Windings) (1)

Major Simplification

- magnetic field of the induced eddy currents neglected.
- This can be problematic at frequencies above (rule-of-thumb) [15]

$$f_{\rm max} = \frac{2.56}{\pi\mu_0 \sigma d^2}$$

Results of considered winding arrangements

f-range $f < f_{max}$ $f > f_{max}$ Error< 5%</td>> 5% (always < 25%)</td>

[15] A. Van den Bossche, V. C. Valchev, "Inductors and Transformers for Power Electronics", CRC Press. Taylor & Francis Group, 2005











Winding Loss Modeling FEM Simulations : Round Windings (Including Litz Wire Windings) (2)



FEM Simulation







Winding Loss Modeling Methods to Decrease Winding Losses (1)



Avoid Orthogonal Flux in Foil Windings

Optimal Solid Wire Thickness



Litz Wire 250 /= 1 m Push this point to 200 higher frequencies! [M¹⁵⁰ [M¹]_d 100 \rightarrow Increase number of strands. 0 10 20 30 40 f[kHz] 50 60 70 80





Winding Loss Modeling Methods to Decrease Winding Losses (2)

Arrangement of Windings





Proximity losses increase in more compact winding arrangements.





Winding Loss Modeling Methods to Decrease Winding Losses (3)

Aluminum vs. Copper [13]

Aluminum (vs. Copper):

- Lighter
- Lower costs
- Lower Conductivity $\sigma = 38 \cdot 10^6 1/(\Omega m)$ (Copper: $\sigma = 58 \cdot 10^6 1/(\Omega m)$)
- → Lower Skin Depth!

Skin- and DC losses higher than in copper conductors.

Proximity losses are lower in aluminum conductors over a wide frequency range. Figure shows a comparison of single round solid conductors in external field.



[13] M. Albach, "Induktive Komponenten in der Leistungselektronik", VDE Fachtagung - ETG Fachbereich Q1 "Leistungselektronik und Systemintegration", Bad Nauheim, 14.04.2011

Example Winding Loss Modeling

Photo & Dimensions





Material Grain-oriented steel (M165-35S) Power Electronic Systems Laboratory



Current Waveform



Demonstration in MATLAB







Outline

- Magnetic Circuit Modeling
- Core Loss Modeling
- Winding Loss Modeling
- Thermal Modeling
- Multi-Objective Optimization
- Summary & Conclusion







Thermal Modeling Motivation & Model (1)







Thermal Modeling Motivation & Model (2)

Model



 \rightarrow Determination of thermal resistors is challenging!



Thermal Modeling Heat Transfer Mechanisms

$$R_{\rm th} = \frac{\Delta T}{P} = f(T)$$

Conduction

Independent of temperature *T* for most materials Difficult to determine interfaces between materials

Convection

Combined effect of conduction and fluid flow Changes with changing absolute temperature (nonlinear) Good empirical calculation approach available

Radiation

Small compared to other mechanisms

Modeling the system is demanding

(nonlinear eq. / to describe which components "sees" the other component).

$$R_{\rm th} = \frac{\Delta T}{R} = \frac{1}{4}$$

 $R_{\rm th} = \frac{\Delta T}{P} = \frac{l}{A\lambda}$

$$q \rightarrow \lambda$$
 A

$$\frac{\Delta T}{P} = \frac{1}{\alpha A}$$

$$P = \mathcal{E}_{eff} A_1 \sigma (T_b^4 - T_a^4)$$





Thermal Modeling Thermal Resistance Calculation : (Natural) Convection (1)

$$R_{\rm th} = \frac{\Delta T}{P} = \frac{1}{\alpha A}$$

 α is a coefficient that is influenced by ...

- ... the absolute temperature,
- ... the fluid property,
- ... the flow rate of the fluid,
- ... the dimensions of the considered surface,
- ... orientation of the considered surface,
- ... and the surface texture.





Thermal Modeling Thermal Resistance Calculation : (Natural) Convection (2)

Empirical solutions known for ...







Thermal Modeling Thermal Resistance Calculation : (Natural) Convection (3)



[16] VDI Heat Atlas, Springer-Verlag, Berlin, 2010





Thermal Modeling Thermal Resistance Calculation : (Natural) Convection (4)

Structure of Empirical Solutions - Example



Vertical Plane

 $Nu = (0.825 + 0.387(Ra \cdot f_1(Pr))^{1/6})^2$

$$f_1 = \left(1 + \left(\frac{0.492}{Pr}\right)^{9/16}\right)^{-16/9}$$

Reference: [16] VDI Heat Atlas, Springer-Verlag, Berlin, 2010





Example ($h = 10 \text{ cm}, T_p = 60 \text{ °C}, T_a = 20 \text{ °C}, A = h \cdot h$) $\Rightarrow R_{\text{th}} = 16.6 \text{ K/W}$

Increase of Winding Surface

$$A_1 \qquad A_2 = A_1 \cdot \pi/2$$





Thermal Modeling

Thermal Resistance Calculation : Conduction

 $R_{\rm th,CW}$

 $R_{\rm th,W1}$

 $T_{\rm W1}$



 $R_{\rm th,W1W2}$



 $R_{\rm th,WA}$

Example Thermal Modeling (1)





(1) Horizontal Plane - Top



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Example Thermal Modeling (2)







(2) Core to Winding



Drawing represents the cross-section of one coil former side (there are total 2 x 4 coil former sides).

Measurement Results

(ΔB =0.18 T, f = 10kHz, triangular)

	Calc.	Meas.	
$P_{\rm core}$	107 °C	112 °C	
$P_{\rm winding}$	100 °C	104 °C	

Quantity Values			
$R_{\rm th.CA} = 3.6 {\rm K}$	/W		
$R_{\rm th,WA}$ = 4.7 K	/W		





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Multi-Objective Optimization – Volume vs. Losses Introduction to the PFC Rectifier (1)

Simplified Schematic



Converter Specifications

Parameter	Variable	Value	
Input Voltage AC	$V_{ m mains}$	230	V
Mains Frequency	$f_{ m mains}$	50	Hz
DC-Voltage	$V_{ m DC}$	650	V
Load Current	$I_{\rm L}$ (nominal)	15.4	А
Switching Frequency	$f_{ m sw}$	8	kHz

Photo of Converter





Multi-Objective Optimization – Volume vs. Losses Introduction to the PFC Rectifier (2)

Simplified Schematic



Filter Specifications

Input Current THD \leq 4 %

Max. current ripple in boost inductors 4 A

LCL filter consists of

three boost inductors

and a damped three-phase *LC* filter.





Multi-Objective Optimization – Volume vs. Losses Introduction to the PFC Rectifier (3)







Multi-Objective Optimization – Volume vs. Losses Modeling LCL Filter (1)

Procedure

- A reluctance model is introduced to describe the electric / magnetic interface, i.e. L = f(i).
- >↓
 2) Core losses are calculated.
 ↓
 3) Winding losses are calculated.
 ↓
 4) Inductor temperature is calculated.

Considered effects

Air gap stray field
Non-linearity of core material
DC Bias
Different flux waveforms
Wide range of flux densities and frequencies
Skin and proximity effect
Stray field proximity effect
Effect of core to magnetic field distribution

Jonas Mühlethaler







Multi-Objective Optimization – Volume vs. Losses Modeling LCL Filter (2)



Volume Calculation

 $0.18 \,\mu F/cm^3$

Power Loss Calculation

 $P = 2\pi f C \tan \delta V^2$



Multi-Objective Optimization – Volume vs. Losses Modeling LCL Filter (3)



Trade-off between damping capacitor size and damping achieved

$$\rightarrow C = C_{d}$$

Optimal damping achieved with [17]

$$R_{\rm d} = \sqrt{2.1 \frac{L_1}{C}}$$

[17] R. W. Erickson and D. Maksimovic, "Fundamentals of Power Electronics", Springer Science+Business Media, LLC, 2004





Multi-Objective Optimization – Volume vs. Losses Optimization of LCL Filter (1)



Constraints concerning boost inductors

max. current ripple $I_{\text{HF,pp,max}}$ max. temperature T_{max} max. volume V_{max}





Multi-Objective Optimization – Volume vs. Losses Optimization of LCL Filter (2)



Constraints concerning LC filter

max. THD of mains current max. temperature T_{max} max. volume V_{max}



Multi-Objective Optimization – Volume vs. Losses Optimization of LCL Filter (3)

Selected Inductor Shape





Filter Design Parameterization

$$X = \begin{pmatrix} l_{g,L1} & l_{g,L2} \\ a_{L1} & a_{L2} \\ N_{L1} & N_{L2} \\ do_{L1} & do_{L2} \\ b_{L1} & b_{L2} \\ t_{L1} & t_{L2} \\ ww_{L1} & ww_{L2} \\ d_{L1} & d_{L2} \end{pmatrix}$$

Filter C Calculation

$$C = \frac{1}{L_1 \omega_0^2} = \frac{1}{L_1 (2\pi f_{\rm sw} \cdot 10^{\frac{A}{40 \, \rm dB}})^2}$$

→ The filter capacitance is calculated to meet the THD constraint.





Multi-Objective Optimization – Volume vs. Losses Optimization of LCL Filter (4)

Simplified current / voltage waveforms for optimization procedure



Expectations

Loss overestimation in L_2 expected.

Loss underestimation in L_1 expected.

Multi-Objective Optimization – Volume vs. Losses Optimization of LCL Filter (5)

Optimization Flow Chart (1)



Boost Inductor

$$L_{2,\min} = \frac{\sqrt{2}|V_{\text{mains}}|}{V_{\text{DC}}/\sqrt{3}}\cos(\pi/6) \cdot \frac{\frac{2}{3}V_{\text{DC}} - \sqrt{2}V_{\text{mains}}}{I_{\text{HF,pp,max}} \cdot f_{\text{sw}}}$$

 $L_{2,\min}$ can be calculated based on the constraint $I_{\text{HF,pp,max.}}$. The maximum current ripple $I_{\text{HF,pp,max}}$ occurs when the fundamental current peaks.

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Multi-Objective Optimization – Volume vs. Losses Optimization of LCL Filter (6)

Optimization Flow Chart (2)



Cost Function

$$F = k_{\rm Loss}P + k_{\rm Volume}V$$






Multi-Objective Optimization – Volume vs. Losses Results – LCL Filter (1)

Filter Losses vs. Filter Volume Pareto Front







Multi-Objective Optimization – Volume vs. Losses Results – LCL Filter (2)







Conclusion

Loss modeling accurate.

THD underestimated (frequency modeling necessary).





Multi-Objective Optimization – Volume vs. Losses Results – LCL Filter (3)



Photo



Conclusion

Loss modeling very accurate.

Current ripple underestimated (frequency modeling necessary).





Multi-Objective Optimization – Volume vs. Losses Results – LCL Filter (4)



Photo of Capacitors

Power Electronic Systems Laboratory



Multi-Objective Optimization – Volume vs. Losses Overall System Optimization (1) – Converter Model



[18] U. Drofenik, G. Laimer, J. W. Kolar, "Theoretical converter power density limits for forced convection cooling", Proc. of. PCIM Europe, Nuremberg, 2005



Multi-Objective Optimization – Volume vs. Losses Overall System Optimization (2) – Optimization Constraints

Variable Value Parameter Max. junction temp. °C $T_{j,\max}$ 125 dm^3 Max. cooling system vol. $V_{\rm CS,max}$ 0.8Heatsink height 4 cm cm^2 Max. area per chip $A_{\rm T,max}/A_{\rm D,max}$ 1 DC link voltage $V_{\rm DC}$ 650V max. DC link voltage overshoot $\Delta V_{\rm DC}$ 50V Fund. peak-peak current $I_{(1),\mathrm{pp}}$ 20.5А

Optimization Constraints

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Multi-Objective Optimization – Volume vs. Losses Overall System Optimization (3) – Converter Pareto Front



A decreasing switching frequency leads to lower losses!



Multi-Objective Optimization – Volume vs. Losses Overall System Optimization (3) – Optimal Designs



Losses of loss-optimized designs



Volume of volumetric-optimized designs



- → In order to get an optimal system design, an overall system optimization has to be performed.
- It is (often) not enough to optimize subsystems independently of each other.

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- Magnetic Circuit Modeling
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Summary & Conclusion Magnetic Circuit Modeling

Air Gap Reluctance Calculation









Summary & Conclusion Core Loss Modeling

"The best of both worlds" (Steinmetz & Loss Map approach)









Summary & Conclusion Winding Loss Modeling

Optimal Solid Wire Thickness







Foil vs. Round Conductors



Gapped cores: 2D approach









Summary & Conclusion Magnetic Design Environment

Core Material Database

Magnetics Design Software



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Summary & Conclusion Multi-Objective Optimization - Next Steps

PFC Rectifier with Input LCL filter



Losses of loss-optimized designs



Filter Pareto Front



Next Steps

Comparison of different rectifier topologies (2-level, 3-level), modulation schemes, etc. on filter size, filter losses.







Thank you !





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